

# Adsorption and Desorption of Water on Tin Dioxide

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**Abstract**—Adsorption isotherms were obtained for water on SnO<sub>2</sub> samples subjected to heat treatment at various temperatures. The monolayer capacity and adsorption constants were determined by Langmuir equation. The enthalpy and entropy of adsorption were determined using the isobar equation.

The dependences of the concentration ( $\bar{C}$ , mol g<sup>-1</sup> SnO<sub>2</sub>) and “strength” ( $K_{\text{dis}}$ ) of acid centers of the SnO<sub>2</sub> surface on the temperature of the preliminary heat treatment of the samples ( $T_{\text{ht}}$  100, 200, 300, 500, 700°C) were found in [1] by pH-metric heterogeneous titration of aqueous suspensions of tin dioxide powders with alkali.

It was of interest to find whether there is a correlation between the parameters found in [1] and the corresponding parameters of water vapor adsorption, and also to calculate the enthalpy ( $\Delta H$ ) and entropy ( $\Delta S$ ) of water desorption.

The adsorption experiments involved measuring the weight gain of SnO<sub>2</sub> samples kept in a desiccator over sulfuric acid. Preliminarily heat-treated SnO<sub>2</sub> samples were kept in a desiccator over 90% sulfuric acid ( $P_{\text{H}_2\text{O}}$  0.005 mm Hg at 20°C [2]). Then they were placed in desiccators over 75, 70, 60, and 40% sulfuric acid (i.e., with a certain partial pressure of water vapor at a given temperature), after which the SnO<sub>2</sub> samples were weighed. The results are given in Table 1.

Adsorption of water vapor on SnO<sub>2</sub> samples is reversible, since the adsorption isotherms coincide with the desorption isotherms.

The adsorption isotherms have a shape typical for monomolecular adsorption [3]. Hence, we treated them using Langmuir equation [4] to determine the numbers of adsorption centers and the adsorption constants.

$$m_{\text{H}_2\text{O}} = m_{\text{max}} \frac{K_{\text{ads}} P_{\text{H}_2\text{O}}}{1 + K_{\text{ads}} P_{\text{H}_2\text{O}}} \quad (1)$$

Here  $m_{\text{H}_2\text{O}}$  is the weight of adsorbed water (g H<sub>2</sub>O/g SnO<sub>2</sub>),  $m_{\text{max}}$  is the monolayer capacity (g H<sub>2</sub>O/g SnO<sub>2</sub>),  $P_{\text{H}_2\text{O}}$  is the water vapor pressure in a desiccator (mm Hg), and  $K_{\text{ads}}$  is the equilibrium constant of adsorption (Henry constant).

The expression for  $K_{\text{ads}}$  can be written as

$$K_{\text{ads}} = \frac{m_{\text{H}_2\text{O}}}{(m_{\text{max}} - m_{\text{H}_2\text{O}}) P_{\text{H}_2\text{O}}} \quad (2)$$

**Table 1.** Experimental data on water vapor adsorption on SnO<sub>2</sub> samples<sup>a</sup>

$W, \% \text{H}_2\text{SO}_4$	$P_{\text{H}_2\text{O}}, \text{mm Hg}$	$T_{\text{ht}} 100^\circ\text{C}$			$T_{\text{ht}} 200^\circ\text{C}$			$T_{\text{ht}} 300^\circ\text{C}$		
		$m_{\text{H}_2\text{O}}^{\text{exp}} \times 10^2$	$(P/m) \times 10^{-1}$	$m_{\text{H}_2\text{O}}^{\text{calc}} \times 10^2$	$m_{\text{H}_2\text{O}}^{\text{exp}} \times 10^2$	$(P/m) \times 10^{-1}$	$m_{\text{H}_2\text{O}}^{\text{calc}} \times 10^2$	$m_{\text{H}_2\text{O}}^{\text{exp}} \times 10^2$	$(P/m) \times 10^{-1}$	$m_{\text{H}_2\text{O}}^{\text{calc}} \times 10^2$
75	0.3	4.5	0.67	4.55	2.8	1.07	2.80	1.4	2.14	1.41
70	0.8	6.2	1.29	6.21	4.4	1.82	4.39	2.6	3.08	2.26
60	2.8	7.4	3.78	7.37	5.8	4.83	5.81	3.9	7.18	3.91
40	9.8	7.8	12.6	7.78	6.4	15.3	6.41	4.6	21.3	4.60

<sup>a</sup>  $m_{\text{H}_2\text{O}}$  is given in g H<sub>2</sub>O/g SnO<sub>2</sub>.

**Table 2.** Parameters derived from experimental data on water vapor adsorption on the SnO<sub>2</sub> surface

$T_{ht}, ^\circ\text{C}$	$m_{\max} \times 10^{-2}$ , g H <sub>2</sub> O/g SnO <sub>2</sub>	$C_{\max} \times 10^3$ , mol H <sub>2</sub> O/g SnO <sub>2</sub>	$K_{\text{ads}}$ , (mm Hg) <sup>-1</sup>	$S_{\text{sp}}$ , m <sup>2</sup> /g SnO <sub>2</sub>	$S_{\text{sp}}^{T=100}/S_{\text{sp}}^T$	$C_{\max}^{T=100}/C_{\max}^T$
100	7.96 ± 0.05	4.4	4.45 ± 0.18	200	1.00	1.00
200	6.68 ± 0.05	3.7	2.40 ± 0.05	175	1.14	1.19
300	4.95 ± 0.05	2.7	1.34 ± 0.05	120	1.67	1.61

$$\frac{P_{\text{H}_2\text{O}}}{m_{\text{H}_2\text{O}}} = \frac{1}{K_{\text{ads}}m_{\max}} + \frac{1}{m_{\max}}P_{\text{H}_2\text{O}}. \quad (3)$$

Equation (3) gives a linear plot of  $P_{\text{H}_2\text{O}}/m_{\text{H}_2\text{O}}$  vs.  $P_{\text{H}_2\text{O}}$ .

We determined  $m_{\max}$  and  $K_{\text{ads}}$  by solving this equation graphically. Below are given  $m_{\max} \times 10^2$  (g H<sub>2</sub>O/g SnO<sub>2</sub>),  $C_{\max} \times 10^3$  (mol H<sub>2</sub>O/g SnO<sub>2</sub>), and  $K_{\text{ads}}$  ( $T_{\text{ht}}$ ): 8.0, 4.4, 4.5 (100°C); 6.7, 3.7, 2.4 (200°C); 5.0, 2.7, 1.3 (300°C).

We also calculated  $m_{\max}$  and  $K_{\text{ads}}$  by the least-squares method (Table 2); they agree with the values found graphically.

Samples with  $T_{\text{ht}}$  500 and 700°C, in contrast to samples with  $T_{\text{ht}}$  100, 200, and 300°C, have the specific surface area smaller by a factor of ~10; therefore, the amount of adsorbed water cannot be determined with a high accuracy. To estimate  $K_{\text{ads}}$  for these samples, we assumed that  $m_{\max}$  is equal to the weight of adsorbed water at a maximal water vapor pressure ( $P_{\text{H}_2\text{O}}$  9.8 mm Hg); thus, it is  $\sim 6 \times 10^{-3}$  g H<sub>2</sub>O/g SnO<sub>2</sub> for samples with  $T_{\text{ht}}$  500°C and  $\sim 2 \times 10^{-3}$  g H<sub>2</sub>O/g SnO<sub>2</sub> for samples with  $T_{\text{ht}}$  700°C.

At  $P_{\text{H}_2\text{O}}$  0.8 mm Hg,  $m_{\text{H}_2\text{O}}$  is  $\sim 1/2m_{\max}$ . Therefore, according to Eq. (3),  $K_{\text{ads}}$  (for samples with  $T_{\text{ht}}$  500 and 700°C) can be estimated as  $1/P_{\text{H}_2\text{O}}$ , and, consequently,  $K_{\text{ads}} \approx 1.25$ .

We tested the reliability of  $m_{\max}$  and  $K_{\text{ads}}$  found for the samples with  $T_{\text{ht}}$  100, 200, and 300°C by calculating  $m_{\text{H}_2\text{O}}^{\text{calc}}$  using Eq. (1) and comparing them with  $m_{\text{H}_2\text{O}}^{\text{exp}}$  (Table 1).

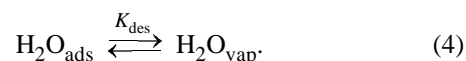
Figure 1 gives a plot of the monolayer capacity ( $C_{\max}$ , mol H<sub>2</sub>O/g SnO<sub>2</sub>) vs. the specific surface area ( $S_{\text{sp}}$ , m<sup>2</sup>/g SnO<sub>2</sub>) of the samples with  $T_{\text{ht}}$  100, 200, and 300°C, found from nitrogen adsorption [4]. This dependence is linear, which allows the landing surface area for a water molecule to be calculated as  $\delta_{\text{H}_2\text{O}}$  8.3 Å<sup>2</sup>. This value is comparable with the value

calculated by the BET equation [4, 5]:  $\delta_{\text{H}_2\text{O}}$  1.091 ( $M_{\text{H}_2\text{O}}/N_{\text{A}}\rho_{\text{H}_2\text{O}})^{2/3} \times 10^{16}$  (where  $M_{\text{H}_2\text{O}}$  is the molar weight of water,  $N_{\text{A}}$  is the Avogadro number, and  $\rho_{\text{H}_2\text{O}}$  is the density of liquid water). With regard to a 20% error, it comprises  $10.5 \pm 2.1$  Å<sup>2</sup>, supporting the results of determining  $C_{\max}$  for water adsorption on SnO<sub>2</sub> samples.

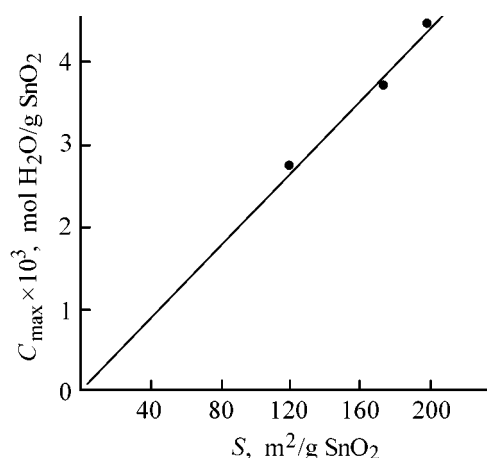
We emphasize that the ratios  $S_{\text{sp}}^{T=100}/S_{\text{sp}}^T$  and  $C_{\max}^{T=100}/C_{\max}^T$  ( $T$  100, 200, and 300°C) virtually coincide (Table 2).

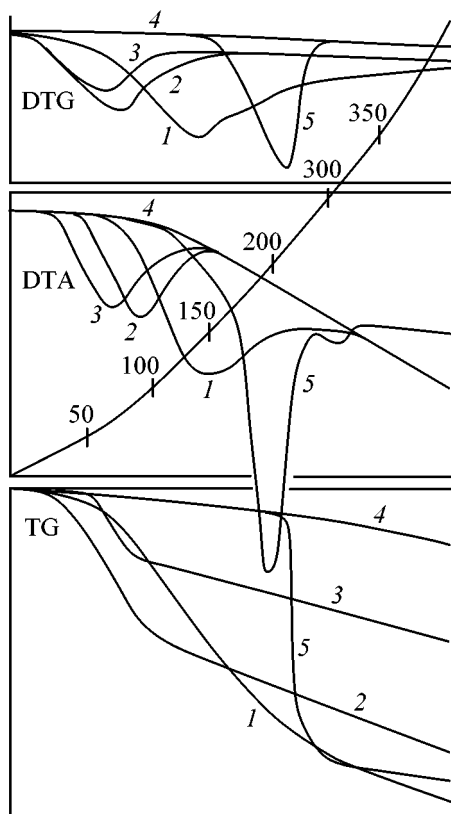
We studied the desorption of water from the surface of air-dry SnO<sub>2</sub> samples with  $T_{\text{ht}}$  100, 200, and 300°C by derivatography with simultaneous recording of DTG, DTA, and TG curves in the temperature range 20–350°C (Fig. 2). The resulting DTA and DTG curves suggest that the desorption is endothermic with the peaks at ~130°C for  $T_{\text{ht}}$  100°C, ~70°C for  $T_{\text{ht}}$  200°C, and ~55°C for  $T_{\text{ht}}$  300°C.

The desorption process can be described by Eq. (4):

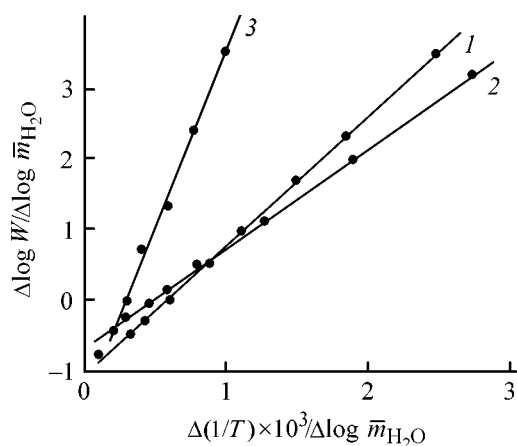


Here  $K_{\text{des}}$  is the desorption constant.


**Fig. 1.** Plot of  $C_{\max}$  vs.  $S_{\text{sp}}$  for SnO<sub>2</sub> samples with  $T_{\text{ht}}$  100, 200, and 300°C.



**Fig. 2.** Derivatograms of  $\text{SnO}_2$  samples: (1) 100°C, (2) 200°C, (3) 300°C, and (4) 500°C; (5)  $\text{CaC}_2\text{O}_4$ .



**Fig. 3.** Plot of  $\Delta \log W / \Delta \log \bar{m}_{\text{H}_2\text{O}}$  vs.  $\Delta(1/T) / \Delta \log \bar{m}_{\text{H}_2\text{O}}$  for  $\text{SnO}_2$  samples. (1) 100°C, (2) 200°C, and (3) 300°C.

$$K_{\text{des}} = \frac{[\text{H}_2\text{O}]_{\text{vap}}}{[\text{H}_2\text{O}]_{\text{ads}}} = \frac{\Delta \bar{m}_{\text{H}_2\text{O}}}{(\bar{m}_{\text{max}} - \Delta \bar{m}_{\text{H}_2\text{O}})} \quad (5)$$

Here  $\Delta \bar{m}_{\text{H}_2\text{O}}$  is the weight loss of an  $\text{SnO}_2$  sample at the temperature  $T$ , and  $\Delta \bar{m}_{\text{max}}$  is the maximal weight loss of an  $\text{SnO}_2$  sample.

The desorption rate depends on both the heating rate and the activation energy of desorption.

We calculated the activation energy of water vapor desorption ( $E_a$ ) by graphic solution of Eq. (6) [6, 7] (Fig. 3).

$$\frac{\Delta \log W}{\Delta \log \bar{m}_{\text{H}_2\text{O}}} = \frac{\Delta E_a}{2.3RT} \frac{\Delta(1/T)}{\Delta \log \bar{m}_{\text{H}_2\text{O}}} - n. \quad (6)$$

Here  $W = \Delta \bar{m}_{\text{H}_2\text{O}} / \Delta t$  is the desorption rate, and  $n$  is the reaction order of water vapor desorption, equal to  $\sim 1$ .

At relatively slow heating ( $\sim 5 \text{ deg min}^{-1}$ ), relatively high desorption rate owing to low activation energy ( $E_a$  7–8 kcal  $\text{mol}^{-1}$ ) of desorption, and low rate of water vapor diffusion from the inner volume of pores, we can suggest that the equilibrium (4) of water distribution between the surface and the vapor is attained at every temperature  $T$  [3]. Hence, it appears possible to calculate  $K_{\text{des}}$  for every temperature  $T$  and to use isobar equation (7) for graphic determination of  $\Delta H_{\text{des}}$  [8] and for subsequent calculation of  $\Delta S_{\text{des}}$ .

$$\log K_{\text{des}} = - \frac{\Delta H_{\text{des}}}{2.3R} \frac{1}{T} + \frac{\Delta S_{\text{des}}}{R}. \quad (7)$$

The calculated values of  $\Delta H_{\text{des}}$  and  $\Delta S_{\text{des}}$  are given below.

	$\Delta H$ , kcal $\text{mol}^{-1}$	$\Delta S$ , cal $\text{mol}^{-1} \text{deg}^{-1}$
$T_{\text{ht}}$ 100°C	11.0	28
$T_{\text{ht}}$ 200°C	11.4	33
$T_{\text{ht}}$ 300°C	13.7	40
Water–vapor	9.6	48
Ice–vapor	11.4	55

The obtained  $\Delta H$  and  $\Delta S$  values suggest that the state of water adsorbed on the  $\text{SnO}_2$  surface does not differ from its state in liquid and crystalline phases. However, as the heat-treatment temperature increases,  $\Delta H_{\text{des}}$  and  $\Delta S_{\text{des}}$  vary in parallel: an increase in  $\Delta S_{\text{des}}$  corresponds to an increase in  $\Delta H_{\text{des}}$ .

## EXPERIMENTAL

Samples of  $\text{SnO}_2$  were weighed on a VLR-200g analytical balance with the accuracy of  $\pm 2 \times 10^{-4} \text{ g}$ . The derivatograms were recorded on a Paulik–Paulik–Erdey derivatograph with 0.2-g samples at a heating rate of  $5 \text{ deg min}^{-1}$ .

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